Lesson 7.5 Real-World Problems: Algebraic Expressions

Solve. Show your work.

- **1.** Daniel's house is located *b* miles from his school. The swimming pool is 3 miles farther from his school. His doctor's office is 4 miles less than twice the distance from home to Daniel's school.
 - a) Write an expression that shows the distance from Daniel's house to the swimming pool.

b) Write an expression that shows the distance from Daniel's house to his doctor's office.

c) If b = 3, is the swimming pool or the doctor's office closer to Daniel's house? How much closer?

- 2. Casey can knit 6m doll dresses in 2 hours.
 - a) Write an expression that shows the number of doll dresses Casey can knit in 5 hours in terms of m.

b) If m = 7, how many doll dresses can Casey knit in 5 hours?

- **3.** At a soccer tournament there are (16x + 30) boys and (5x 12) more girls than boys.
 - a) How many children are there at the tournament in terms of x?

b) If x = 5, how many girls are at the tournament?

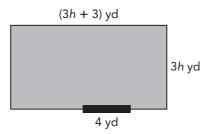
- **4.** Adam sold 16p newspapers in the morning. He sold $\frac{3}{4}$ as many newspapers in the afternoon as he did in the morning. He sold 20 more newspapers in the evening than in the afternoon.
 - a) How many newspapers did Adam sell altogether in terms of p?

b) If p = 3, how many newspapers did Adam sell altogether?

5. Alicia, Jamar, and Tia collect dimes for charity. Alicia collects (3k + 4) dimes. Jamar collects twice as many dimes as Alicia. Tia collects 4(5 + 6k) dimes. How many dimes do they collect altogether in terms of k?

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6. The width of a rectangular field is 3h yards and its length is 3 yards longer than the width. The field has a fence around its perimeter with a gate 4 yards wide, as shown below.



- a) Write an expression for the perimeter of the rectangular field in terms of *h*, excluding the width of the gate.
- **b)** It costs \$28 per yard to fence the field, excluding the gate. Write an expression that represents the cost of fencing the field.
- c) If h = 5, find the cost of the fencing, excluding the gate.
- 7. Moesha is (3g + 1) years old and Shanti is twice Moesha's age.
 - a) Find the sum of the ages of Moesha and Shanti in 2 years' time.
 - **b)** How old will Shanti be when Moesha's age is twice her present age?
 - c) Find how old Moesha and Shanti were 4 years ago if g = 5.

- **22.** 2(7 + 3x) or 2(3x + 7)
- **23.** 7(3h + 4)
- **24.** 3(6k + 5)
- **25.** 3y 9 + 10 + 6y + 48y 120 + 30 6y= 51y - 89
- **26.** Both expressions are equal to 15w + 54. Yes, the two expressions are equivalent.
- **27.** a) 3(5x 8) miles
 - **b)** $3(5 \cdot 15 8) = 201$ The train travels 201 miles.
- Total amount = 2(3w + 8) + 3(4w 3)28. a) = (18w + 7) dollars
 - $18 \cdot 4 + 7 = 79$
- Mrs. Young paid \$79. **29.** 4(15h - 3) = 60h - 12(60h - 12) + (10h + 46) + (14h - 16)

$$= 84h + 18$$

 $(84h + 18) \div 6 = 14h + 3$

$$14 \cdot 9 + 3 = 129$$

129 centimeters

- **30.** a) 6(2d-3) = (12d-18) centimeters
 - **b)** 8(2d 3) = (16d 24) centimeters
 - c) Difference: 2(2d 3) $2(2 \cdot 8 - 3) = 26$ centimeters

Lesson 7.5

- **1. a)** (b + 3) miles
 - **b)** (2b 4) miles
 - The doctor's office is closer. c) It is 2 miles closer.
- **2.** a) 1 hour $\rightarrow 6m \div 2 = 3m$ $5 \text{ hours} \rightarrow 5 \times 3m = 15m$ Casey can knit 15m doll dresses in 5 hours.
 - **b)** $15 \cdot 7 = 105$ Casey can knit 105 doll dresses in 5 hours.
- **3. a)** Number of girls: (16x + 30) + (5x 12)= (21x + 18)Total = (16x + 30) + (21x + 18)= (37x + 48)

There are (37x + 48) children at the tournament.

- **b)** Number of girls: (21x + 18) $21 \cdot 5 + 18 = 123$ girls
- **4. a)** Afternoon: $\frac{3}{4} \cdot 16p = 12p$ Evening: 12p + 20Total = 16p + 12p + (12p + 20)= 40p + 20

Adam sold (40p + 20) newspapers altogether.

b) $40 \cdot 3 + 20 = 140$ newspapers

5. (3k + 4) + 2(3k + 4) + 4(5 + 6k)= 33k + 32

They collect (33k + 32) dimes altogether.

- **6. a)** (12h + 2) yards
 - **b)** The cost is 28(12h + 2) dollars.
 - $28(12 \cdot 5 + 2) = 1,736$ The cost is \$1,736.
- 7. a) (3g + 1) + 2(3g + 1) + 2 + 2= 9g + 7The sum of their ages is (9g + 7) years.
 - **b)** 2(3g + 1) + (3g + 1)= 9g + 3Shanti will be (9g + 3) years old.
 - c) Moesha's age: 3g + 1 4 $= 3 \cdot 5 + 1 - 4 = 12$ years Shanti's age: 2(3g + 1) - 4 $= 2 \cdot 16 - 4 = 28$ years

Brain @ Work

- 1. a) $\frac{1}{w}$ of the pool
 - **b)** $\frac{1}{w+6}$ of the pool
 - c) $4\left(\frac{1}{w} + \frac{1}{w+6}\right)$ of the pool
- 2. a) $\frac{1}{3v+2}$ of the house
 - **b)** $2\left(\frac{1}{3y+2+5}\right) = \frac{2}{3y+7}$ of the house
 - **c)** $3\left(\frac{1}{3y+2} + \frac{1}{3y+7}\right)$ of the house

Cumulative Practice

for Chapters 4 to 7+++

- **1.** 135
- **3.** 2:5
- **5.** 5 : 3
- **7.** 76% 9. 65%
- **2.** 6 **4.** 8 : 13
- **6.** 4:3 8. 109%
- **11.** 0.09
- 22
- **14.** $1\frac{1}{5}$
- **15.** 43.2 quarts
- **16.** 36 minutes
- **17.** 25
- **18.** 18
- **19.** 49
- **20.** 15 **22.** 9 + 5*y*
- **21.** 7w + 5**23.** 24*q* – 12
- **24.** 38 + 52y
- **25.** 4(4g + 1)
- **27.** 6*p* + 7
- **26.** 7(7 2h)
- **28.** 8 notebooks $\rightarrow y$ dollars 2 notebooks $\rightarrow \frac{y}{4}$ dollars
- **29.** Nails $\rightarrow m + 20$ Bolts $\rightarrow 2m + 30$

Total \rightarrow 3m + 50 nails and bolts